

The Essentials of Computer Organization and Architecture

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Chapter 2 Instructor's Manual

Chapter Objectives

Chapter 2, Data Representation, provides thorough coverage of the various means computers use to represent both numerical and character information. Addition, subtraction, multiplication, and division are covered once the reader has been exposed to number bases and the typical numeric representation techniques, including one's complement, two's complement, and BCD. In addition, EBCDIC, ASCII, and Unicode character representations are addressed. Fixed and floating point representation are also introduced. Codes for data recording and error detection and correction are covered briefly.

This chapter should be covered after Chapter 1, but before Chapters 4 through 11.

Lectures should focus on the following points:

- **Number systems.** Most students have been exposed to positional number systems and different bases. However, these concepts are crucial to understanding the remainder of Chapter 2, so they should be covered in detail.
- **Decimal to binary conversions.** Because the binary number system translates easily into electronic circuitry, it is important to become familiar with how computer represent values.
- **Signed versus unsigned numbers.** Representing unsigned numbers in binary form is much less complicated than dealing with signed numbers.
- **Signed integer representation.** There are basically three methods for representing signed numbers: signed magnitude, one's complement, and two's complement. Each of these methods should be covered, with the focus on signed magnitude and two's complement notations.
- **Binary arithmetic.** Although people do not often add binary values, performing binary addition and subtraction helps to reinforce the concepts necessary for understanding data representation. In particular, these operations illustrate the dangers of overflow conditions.
- **Floating point representation.** Computers must be able to represent floating point numbers, and there are numerous possible formats for doing so. Potential errors that may result from the limitations of the representation are also important to discuss.
- **Character representation.** ASCII, EBCDIC, Unicode and BCD are all important character codes. Lectures should emphasize the similarities and differences among these codes.
- **Codes for data recording and transmission.** When binary data is written to some sort of medium or transmitted over long distances, the binary one's and zero's can become

blurred. Some sort of encoding is necessary to ensure that characters are properly encoded in these situations.

• **Error detection and correction.** Regardless of the coding method used, no communications channel or storage medium is error-free. Although simple parity bits can help to detect errors, more complicated codes, including cyclic redundancy checks and Hamming codes, and are often necessary for sophisticated error detection and correction.

Required Lecture Time

Chapter 2 can typically be covered in 6 lecture hours, depending on how detailed one wishes to go into recording and transmission codes and error detection and correction. We suggest that the focus be on integer, floating-point, and character representation, with emphasis given to complement notation. If time permits, data recording and transmission codes and error detection and correction codes can be covered.

Lecture Tips

Teachers should spend time explaining the ranges allowed by the different representation formats. For example, if we are using 4 bits to represent unsigned integers, we can represent values from 0 to 15. However, if we are using signed magnitude representation, the bits are interpreted differently, and the possible range is from -7 to +7. Make sure students understand why it is not possible to represent +9 or +10, as these will be seen as -1 and -2 respectively.

Converting unsigned whole numbers tends to be relatively straight-forward, but signed numbers and fractions tend to be more difficult. In particular, complement systems confuse students. They often think that all numbers have to be negated to be represented. For example, if a student is asked how a computer, using two's complement representation, would represent -6 (assuming 4-bit values), they answer: 1010 (take 0110, toggle each bit and add 1). This is, of course, the correct answer. However, if that student is asked how the computer using two's complement representation would represent +6, they will often do exactly the same thing, giving the same answer. Teachers need to be sure that students realize representing positive numbers does not require any "conversion". It is only when a number is negative that two's complement, signed magnitude, and one's complement representations are necessary.

Instructors should spend time on overflow and look at several examples so that students can fully appreciate the consequences. Students find it difficult to understand why one time a carry results in overflow, but yet another carry may not result in overflow.

Floating point representation is fairly straight-forward, but students often have difficulty with the format and the bias.

Answers to Exercises

♦ 1. Perform the following base conversions using subtraction or division-remainder:

♦ a. 458₁₀ = _____ 3
♦ b. 677₁₀ = _____ 5

```
• c. 1518_{10} = 27

• d. 4401_{10} = 29

Ans.

a. 121222_3 b. 10202_5 c. 4266_7 d. 6030_9
```

2. Perform the following base conversions using subtraction or division-remainder:

	a. 588 ₁₀ =	3		
	b. 2254 ₁₀ =	= 5		
	c. 652 ₁₀ =	= 7		
	d. 3104 ₁₀ =	= 9		
Ans				
	a. 210210 ₃	b. 33004 ₅	c. 1621 ₇	d. 4228 ₉

3. Convert the following decimal fractions to binary with a maximum of six places to the right of the binary point:

♦ a. 26.78125
♦ b. 194.03125
♦ c. 298.796875
♦ d. 16.1240234375
Ans.
a. 11010.11001
b. 11000010.00001
c. 100101010.110011
d. 10000.000111

4. Convert the following decimal fractions to binary with a maximum of six places to the right of the binary point:

```
a. 25.84375 b. 57.55 c. 80.90625 d. 84.874023
Ans.
a. 11001.11011 b. 111001.100011
c. 1010000.11101 d. 1010100.110111
```

5. Represent the following decimal numbers in binary using 8-bit signed magnitude, one's complement and two's complement:

 ♦ a. 77
 ♦ b. -42
 c. 119
 d. -107

Ans.

 a. Signed magnitude: 01001101 One's complement: 01001101 Two's complement: 01001101
 b. Signed magnitude: 10101010 One's complement: 11010101 Two's complement: 11010110
 c. Signed magnitude: 01110111 One's complement: 01110111 Two's complement: 01110111

Page 3 Last Updated: November 2003 d. Signed magnitude: 11101011 One's complement: 10010100 Two's complement: 10010101

6. Using a "word" of 3 bits, list all of the possible signed binary numbers and their decimal equivalents that are representable in:

a. Signed magnitude b. One's complement c. Two's complement Ans. a. 011 to 111, or +3 to -3 b. 011 to 100, or +3 to -3 c. 011 to 100, or +3 to -4

7. Using a "word" of 4 bits, list all of the possible signed binary numbers and their decimal equivalents that are representable in:

a. Signed magnitude b. One's complement c. Two's complement Ans. a. 0111 to 1111, or +7 to -7 b. 0111 to 1000, or +7 to -7 c. 0111 to 1000, or +7 to -8

8. From the results of the previous two questions, generalize the range of values (in decimal) that can be represented in any given *x* number of bits using:

e's complement c. Two's complemen	t
	e's complement c. Two's complemen

9. Given a (very) tiny computer that has a word size of 6 bits, what are the smallest negative numbers and the largest positive numbers that this computer can represent in each of the following representations?

🔷 a.	One's complement b.	Two's complement	
Ans.			
a.	Largest Positive: 011111 ₂ (31)	Smallest Negative:	1000002 (-31)
b.	Largest Positive: 011111 ₂ (31)	Smallest Negative:	1000002 (-32)

10. You have stumbled on an unknown civilization while sailing around the world. The people, who call themselves Zebronians, do math using 40 separate characters (probably because there are 40 stripes on a zebra). They would very much like to use computers, but would need a computer to do Zebronian math, which would mean a computer that could represent all 40 characters. You are a computer designer and decide to help them. You decide the best thing is to use BCZ, Binary Coded Zebronian (which is like BCD except it

codes Zebronian, not Decimal). How many bits will you need to represent each character if you want to use the minimum number of bits?

Ans.

40 characters need to be represented by binary coded Zebronian (BCZ), so you will need 6 bits. 5 bits would only give you 32 (2⁵) unique characters. Note that 6 bits would allow you to represent 64 characters.

 11. Perform the following binary multiplications:

 \bullet a. 1100
 b. 10101
 c. 11010

 $\times 101$ $\times 111$ $\times 1100$

 Ans.
 a. 111100
 b. 10010011
 c. 100111000

12. Perform the following binary multiplications:

a.	1011	b.	10011	c.	11010	
	<u>× 101</u>		<u>× 1011</u>		<u>× 1011</u>	
Ans.						
a.	1000010		b. 1111	001	c. 100011110	

13. Perform the following binary divisions:

 • a. 101101 ÷ 101
 b. 10000001 ÷ 101
 c. 1001010010 ÷ 1011

 Ans.
 a. 1001
 b. 1101
 c. 110110

14. Perform the following binary divisions:

a. 11111101 ÷ 1011 b. 110010101 ÷ 1001 c. 1001111100 ÷ 1100 Ans. a. 10111 b. 101101 c. 110101

• 15. Use the double-dabble method to convert 10212_3 directly to decimal. (Hint: you have to change the multiplier.)

Ans.

 10212_3 converted to decimal is 104 as shown below:

1 2 0 1 2 3 9 33 102 +0 +2 +1 +2 3 11 104 34 <u>x3</u> 9 $\frac{x3}{3}$ x3 x3 33 102

16. Using signed-magnitude representation, complete the following operations:

- 17. Suppose a computer uses 4-bit one's complement numbers. What value will be stored in the variable j after the following pseudocode routine terminates?

```
0 \rightarrow j // \text{Store 0 in } j.
-3 \rightarrow k // \text{Store -3 in } k.
while k \neq 0
j = j + 1
k = k - 1
end while
```

Ans.

J	(Binary)	Κ	(Binary)
-			
0	0000	-3	1100
1	0001	-4	1011 (1100 + 1110) (where last carry is added to sum doing 1's complement addition)
2	0010	-5	1010 (1011 + 1110)
3	0011	-6	1001 (1010 + 1110)
4	0100	-7	1000 (1001 + 1110)
5	0101	7	0111 (1000 + 1110) (This is overflow but you can ignore)
6	0110	6	0110
7	0111	5	0101
-7	1000	4	0100
-6	1001	3	0011
-5	1010	2	0010
-4	1011	1	0001
-3	1100	0	0000

- 18. If the floating-point number storage on a certain system has a sign bit, a 3-bit exponent and a 4-bit significand:
 - a. What is the largest positive and the smallest positive number that can be stored on this system if the storage is normalized? (Assume no bits are implied, there is no biasing, exponents use two's complement notation, and exponents of all zeros and all ones are allowed.)
 - b. What bias should be used in the exponent if we prefer all exponents to be non-negative? Why would you choose this bias?

Ans.

a. Largest Positive:	0.1111 ₂ x 2 ³	$P = 111.1_2 = 7.5$
Smallest Positive:	0.1 ₂ x 2 ⁻⁴	$= .00001_2 = 1/32 = 0.03125$

- b. For all non-negative exponents, we would need a bias of 4.
- 19. Using the model in the previous question, including your chosen bias, add the following floating-point numbers and express your answer using the same notation as the addend and augend:

0	1	1	1	1	0	0	0
0	1	0	1	1	0	0	1

Calculate the relative error, if any, in your answer to the previous question.

Ans.

0 1 1 1 1 0 1 0 Error = 2.4%

- 20. Assume we are using the simple model for floating-point representation as given in this book (the representation uses a 14-bit format, 5 bits for the exponent with a bias of 16, a normalized mantissa of 8 bits, and a single sign bit for the number):
 - a. Show how the computer would represent the numbers 100.0 and 0.25 using this floating-point format.
 - b. Show how the computer would add the two floating-point numbers in part a by changing one of the numbers so they are both expressed using the same power of 2.
 - c. Show how the computer would represent the sum in part b using the given floatingpoint representation. What decimal value for the sum is the computer actually storing? Explain.

a.
$$100.0 = 0 1 0 1 1 1 1 1 0 0 0 0 0$$

 $0.25 = 0 0 1 1 1 1 1 1 0 0 0 0 0 0 0$
b. Adding in part(a) we get: $.11001 \times 2^7 = .11001 \times 2^7 + .1 \times 2^{-1} = .000000001 \times 2^7 = .110010001 \times 2^7$
c. The sum from part b in the given floating point notation is:
 $0 1 0 1 1 1 1 1 1 0 0 1 0 0 0$
which is $.11001 \times 2^7 = .1100100 = 100$.

21. What causes divide underflow and what can be done about it?

Ans.

Divide underflow is happens when the divisor is much smaller than the dividend. The computer may not be able to reconcile the two numbers of greatly different magnitudes, and thus the smaller gets represented by zero. The result of the division then becomes the equivalent of a division by zero error. Compare this to underflow, which is a condition that can occur when the result of a floating point operation would be smaller in magnitude

(closer to zero, either positive or negative) than the smallest representable quantity. Division underflow could be avoided by using repeated subtraction.

22. Why do we usually store floating-point numbers in normalized form? What is the advantage of using a bias as opposed to adding a sign bit to the exponent?

Ans.

There are two reasons to use normalized form. First, normalized form creates a standard so each floating point value has a unique binary representation. Second, with normalized numbers, we can "imply" the high-order 1 in the significand, giving us an extra bit of accuracy for "free". Using a bias allows an extra bit position to be used for the magnitude of the exponent, as no sign bit is required.

23. Let $a = 1.0 \times 2^9$, $b = -1.0 \times 2^9$ and $c = 1.0 \times 2^1$. Using the floating-point model described in the text (the representation uses a 14-bit format, 5 bits for the exponent with a bias of 16, a normalized mantissa of 8 bits, and a single sign bit for the number), perform the following calculations, paying close attention to the order of operations. What can you say about the algebraic properties of floating-point arithmetic in our finite model? Do you think this algebraic anomaly holds under multiplication as well as addition?

$$b + (a + c) =$$

 $(b + a) + c =$

Ans.

 $b + (a + c) = b + [1.0 \times 2^9]$ $1.0 \ge 2^{1}$ + b + [1.0 x 2⁹ _ $.00000001 \times 2^9$) 1.00000001 x 2⁹ b + $0.100000001 \ge 2^{10}$ (but we can only have 8 bits in the mantissa) = = b + $0.1000000 \text{ x } 2^{10}$ = b + 1.0 x 2⁹ = (-1.0 x 2⁹) + (1.0 x 2⁹) = 0 $(b + a) + c = [(-1.0 \times 2^9) + (1.0 \times 2^9)] + c$ = 0 + c= C $= 1.0 \times 2^{1} = 10$

When one number is significantly larger than the other, round off error occurs due to the limited number of bits in the mantissa. Multiplication does not require the values to be expressed with the same powers of 2, and does not suffer from this problem.

24. a. Given that the ASCII code for A is 1000001, what is the ASCII code for J?

b. Given that the EBCDIC code for A is 1100 0001, what is the EBCDIC code for J? Ans.

a. If A = 1000001, then J = 1001010

b. If $A = 1100\ 0001$, then $J = 1101\ 0001$

25. Assume a 24-bit word on a computer. In these 24 bits, we wish to represent the value 295.

- a. If our computer uses even parity, how would the computer represent the string 295?
- b. If our computer uses 8-bit ASCII and even parity, how would the computer represent the string 295?
- c. If our computer uses packed BCD, how would the computer represent the number +295?

Ans.

Binary Value	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	1	0	0	1	1	1
ASCII	1	0	1	1	0	0	1	0	0	0	1	1	1	0	0	1	0	0	1	1	0	1	0	1
Packed BCD	0	0	0	0	0	0	0	0	0	0	1	0	1	0	0	1	0	1	0	1	1	1	0	0

26. Decode the following ASCII message, assuming 7-bit ASCII characters and no parity: 1001010 1001111 1001000 1001110 0100000 1000100 1001111 1000101 (Blue indicates a correction was made from what is in the textbook.)

Ans.

- 100 1010 = J 100 1111 = O 100 1000 = H 100 1110 = N 010 0000 = space 100 0100 = D 100 1111 = O 100 0101 = E
- 27. Why would a system designer wish to make Unicode the default character set for their new system? What reason(s) could you give for not using Unicode as a default?

Ans.

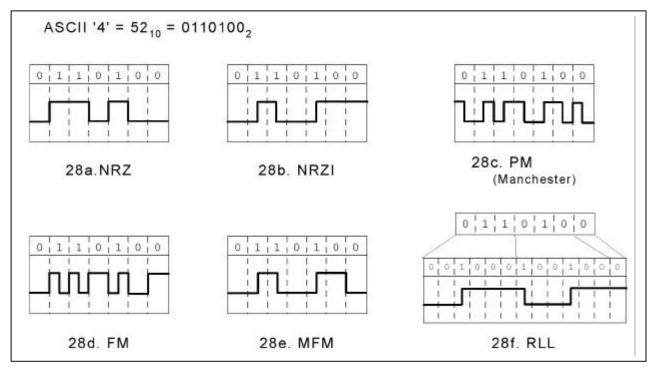
(Hint: Think about language compatibility versus storage space.) Although Unicode would make systems compatible (with each other and with other ASCII systems(), it requires 16 bytes for storage compared to the 7 or 8 required by ASCII or EBCDIC.

28. Write the 7-bit ASCII code for the character 4 using the following encoding:

- a. Non-return-to-zero
- b. Non-return-to-zero-invert
- c. Manchester Code
- d. Frequency modulation
- e. Modified frequency modulation
- f. Run length limited

(Assume 1 is "high," and 0 is "low.")

Ans.



29. Why is NRZ coding seldom used for recording data on magnetic media?

Ans.

NRZ coding is seldom used for recording data on magnetic media because it has unacceptably high error rates and not contain sufficient transitions to keep read/write heads synchronized.

30. Assume we wish to create a code using 3 information bits, 1 parity bit (appended to the end of the information), and odd parity. List all legal code words in this code. What is the Hamming distance of your code?

Ans.

 The legal code words are:

 0001
 1000

 0011
 1011

 0100
 1101

 0111
 1110

and the Hamming distance of these code words is 1.

31. Are the error-correcting Hamming codes systematic? Explain.

Ans.

Error-correcting Hamming codes interleave additional error-checking (parity) bits into the actual information bits, but do not append these bits. In a systematic code, the first k bist of the codeword must be the same as the corresponding message bits (the parity bits must be appended), so by definition, Hamming codes are not systematic.

32. Compute the Hamming distance of the following code:

Ans.

4

33. Compute the Hamming distance of the following code:

Ans.

4

- 34. Suppose we want an error-correcting code that will allow all single-bit errors to be corrected for memory words of length 10.
 - a. How many parity bits are necessary?
 - b. Assuming we are using the Hamming algorithm presented in this chapter to design our error-correcting code, find the code word to represent the 10-bit information word: 1001100110.

Ans.

a. $m + r + 1 \le 2^{r}$ $10+r+1 \le 2^{r}$ $11+r \le 2^{r}$

which implies that r is 4

b. The code word for 1001100110 is found as follows:

Parity bit 1 checks 1,3,5,7,9,11,13, so Bit 1 must be 0 (assuming even parity) Parity bit 2 checks 2,3,6,7,10,11,14, so Bit 2 must be 0 Parity bit 4 checks 4,5,6,7,12,14, so Bit 4 must be 1 Parity bit 8 checks 8,9,10,11,12,13,14, so Bit 8 must be 1

35. Suppose we are working with an error-correcting code that will allow all single-bit errors to be corrected for memory words of length 7. We have already calculated that we need 4 check bits, and the length of all code words will be 11. Code words are created according to the Hamming Algorithm presented in the text. We now receive the following code word:

10101011110

Assuming even parity, is this a legal code word? If not, according to our error-correcting code, where is the error?

Ans.

The error is in bit 5.

36. Repeat exercise 35 using the following code word:

01111010101

Ans.

 $\underbrace{0}_{11} \underbrace{1}_{10} \underbrace{1}_{9} \underbrace{1}_{8} \underbrace{1}_{7} \underbrace{0}_{6} \underbrace{1}_{5} \underbrace{0}_{4} \underbrace{1}_{3} \underbrace{1}_{2} \underbrace{1}_{1}$

Bit 1 checks 1,3,5,7,9 and 11, but this is an odd number of 1's \rightarrow error Bit 2 checks 2,3,6,7,10, and 11, which is an odd number of 1's \rightarrow error Bit 4 checks 4,5,6, and 7, which is an even number of 1's \rightarrow ok Bit 8 checks 8,9,10, and 11, which is an odd number of 1's \rightarrow error Since errors occur in bit positions 1, 2, and 8, the error is in bit number 1+2+8=11

37. Name two ways in which Reed-Soloman coding differs from Hamming coding.

Ans.

Reed-Soloman codes are formed by polynomial division operating on whole characters (symbols), and are thus block-level codes. Hamming codes are bit-parity operations over certain defined bits of a symbol (so these are bit-level codes). Reed-Soloman codes are good at detecting and correcting burst errors, whereas Hamming codes are not.

38. When would you choose a CRC code over a Hamming code? A Hamming code over a CRC? *Ans.*

CRCs are useful for checking data sent over telecommunication lines. If a CRC error occurs, a retransmission is requested. You would choose a CRC when you can ask for retransmission and do not want to sustain the (space and time) overhead of Hamming codes. Hamming codes are good at forward error correction: they can correct errors when retransmission is not possible, such as when data is stored on a disk. CRC is better than Hamming in terms of speed, but Hamming is better than CRC in terms of complexity (Hamming codes do not require complex circuits).

39. Find the quotients and remainders for the following division problems modulo 2.

a. $1010111_2 \div 1101_2$ b. $1011111_2 \div 11101_2$ c. $1011001101_2 \div 10101_2$

d.
$$111010111_2 \div 10111_2$$

Ans.

a. 1101 Remainder 110 c. 100111 Remainder 110 b. 111 Remainder 1100d. 11001 Remainder 1000

40. Find the quotients and remainders for the following division problems modulo 2.

a.	$1111010_2 \div 1011_2$
b.	$1010101_2 \div 1100_2$
C.	$1101101011_2 \div 1010^{\circ}$

c. $1101101011_2 \div 10101_2$ d. $1111101011_2 \div 101101_2$

Ans.

a. 1101 Remainder 101	b. 1100 Remainder 101
c. 111011 Remainder1100	d. 11010 Remainder 1001

41. Using the CRC polynomial 1011, compute the CRC code word for the information word, 1011001. Check the division performed at the receiver.

Ans.

Codeword: 1011001011

42. Using the CRC polynomial 1101, compute the CRC code word for the information word, 01001101. Check the division performed at the receiver.

Ans.

The codeword is 01001101100. Dividing this by 1101 modulo 2 should yield a zero remainder.

Append three 0s to the end of the information word and divide:

$$\begin{array}{c|c} 1101 \hline 01001101000 \\ \hline 1101 \\ \hline 1001 \\ \hline 1000 \\ \hline 1101 \\ \hline 1011 \\ \hline 1011 \\ \hline 1101 \\ \hline 1100 \\ \hline 1101 \\ \hline 100 \\ --> \text{ remainder} \end{array}$$

The information word (with appended zeros) + remainder = codeword so we have: 01001101000 + 100 = 01001101100

To check the division:

1101 01001101	100	
1101		
1001		
1101		
1000		
1101		
1011		
1101		
1101		
1101		
0000	>	remainder

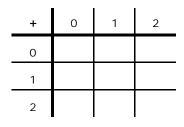
*43. Pick an architecture (such as 80486, Pentium, Pentium IV, SPARC, Alpha, or MIPS). Do research to find out how your architecture approaches the concepts introduced in this chapter. For example, what representation does it use for negative values? What character codes does it support?

Ans.

No answer.

Sample Exam Questions

1. Fill in the following addition table for base 3.



Ans.

Row 1: 0, 1, 2 Row 2: 1, 2, 0 Row 3: 2, 0, 1

2. Perform the following base conversions using subtraction or division-remainder:



3. Show the representation of -16 (assuming 8-bit registers) using:

a. signed-magnitude representation

- b. signed-1's complement
- c. signed-2's complement

Ans.

- a. 10010000
- b. 11101111
- c. 11110000
- 4. Given the 8-bit binary number: **10011101**

What decimal number does this represent if the computer uses:

a. signed-magnitude representation

- b. signed-1's complement
- c. signed-2's complement

Ans.

- a. 29
- b. 98
- с. 99

Assuming 2's complement 8-bit representation, consider the following: 5.

+70= 010001102

+80 010100002 =

 10010110_{2} Is this correct? Why or why not?

Ans.

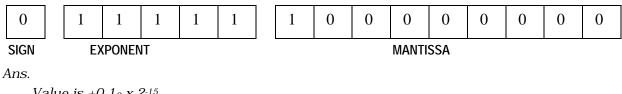
No. The result is a different sign than the two numbers we are adding so overflow has occurred.

If a computer uses signed-2's complement representation and 8 bit registers, what range 6. of integers can this computer represent? What range of integers can the computer represent if it is using signed magnitude representation?

Ans.

Range (signed 2's complement): - 128 to + 127 Range (signed magnitude): -127 to +127

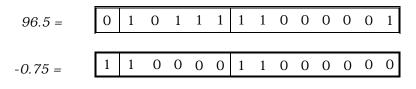
7. A 15-bit floating point number has 1 bit for the sign of the number, 5 bits for the exponent and 9 bits for the mantissa (which is normalized). Numbers in the exponent are in signed magnitude representation. No bias is used and there are no implied bits. Show the representation for the smallest positive number this machine can represent.



Value is +0.1₂ x 2⁻¹⁵.

8. Assume we are using the simple model for floating-point representation as given in the book (the representation uses a 14-bit format, 5 bits for the exponent with a bias of 16, a normalized mantissa of 8 bits, and a single sign bit for the number). Show how the computer would represent the numbers 96.5 and -0.75 using this floating-point format.

Ans.



9. Find the Hamming distance d for the following code: {01010,10101,11111,00000,00110} *Ans*.

The distance is 2.

10.	a. To detect e single	bit errors, we need a Hamming distance d =	
	b. To correct e singl	-bit errors, we need a Hamming distance d =	·
Ans.			
	a. e+1	b. 2e + 1	

- 11. a. Suppose we want an error correcting code that will allow all single-bit errors to be corrected for memory words of length 11. How many check bits are necessary?
 - b. Suppose we are now working with memory words of length 8. We have already calculated that we need 4 check bits, and the length of all codewords will be 12. We now receive the following code word:

010111101110

Is this a legal codeword, assuming odd parity? If not, where is the error?

Ans.

- a. $11+r+1 \le 2^r$ implies an r of 4.
- Bit 1 checks 1,3,5,7,9 and 11, but this is an even number of 1's \rightarrow error Bit 2 checks 2,3,6,7,10, and 11, which is an odd number of 1's \rightarrow ok Bit 4 checks 4,5,6, 7, and 12, which is an odd number of 1's \rightarrow ok Bit 8 checks 8,9,10, 11 and 12, which is an odd number of 1's \rightarrow ok Since an error occurs in bit position 1, this is where the error is.
- 12. Given that the ASCII code for the character "A" is 1000001, the ASCII code for "H" would be:

a. 1010101 b. 1110101 c. 1000100 d. 1001000 e. none of these

Ans.

The correct answer is D.

13. How many base-3 digits does it take to obtain as many combinations as can be done with 5 binary digits?

a.eleven		b. three	c.	four
d.five	e.	this can't be done		

Ans.

The correct answer is C.

- 14. ASCII, EBCDIC, and Unicode are translated into other codes before they are transmitted or recorded. These data encoding methods include all but which of the following:
 - a. non-return-to-zero encoding
- b. Manchester coding
- c. non-return-to-zero-invert encoding d. run-length-limited coding
- e. all of these are encoding methods for recorded or transmitted data

Ans.

The correct answer is E.

TRUE OR FALSE.

- ____ 1. BCD stands for Binary Coded Decimal and encodes each digit of a decimal number to an 8-bit binary form.
- 2. Unicode is a 16-bit code, occupying twice the disk space for text as ASCII or EBCDIC would require.
- 3. Hamming codes, used for error detection and correction, are useful for burst errors (where we could reasonably expect multiple adjacent bits to be incorrect); Reed-Soloman coding is more useful for random errors (where one can reasonably expect errors to be rare events).
- 4. A signed-magnitude integer representation includes more negative numbers than it does positive ones.
- 5. CRCs are useful when you can ask for retransmission; Hamming codes are good when retransmission is not possible, such as when data is stored on a disk.

Ans.

1. True 2. True 3. False 4. True 5. False